## COMP278 MIDTERM

NAME $\qquad$

Complete this exam within 50 minutes. Write legibly and check your work. Good luck!

1. Binary arithmetic (20\%)

Perform the following basic arithmetic operations.
(1) $(10010011)_{2}+(11010101)_{2}$.
(2) $(100010110)_{2}-(1110010)_{2}$.
$\qquad$
2. Number representation ( $20 \%$ )

Convert the following numbers to the specified bases:
(1) $(33662575655)_{8}$ in binary.
(2) The number above, $(33662575655)_{8}$, in hexadecimal.
(3) (170) ${ }_{10}$ in binary.
(4) The number above, ( 170$)_{10}$, in octal.

## 3. Combinational circuit design ( $60 \%$ )

Given a 4-bit binary number A, design a circuit that outputs whether the number of bits set to 1 equals the number of bits set to 0 . For example, 0010 has three bits set to 0 and one bit set to 1 . Thus, for 0010 , the circuit outputs 0 to indicate the number of 0 bits is not equal to the number of 1 bits.
(1) Draw the truth table for this circuit.

Label inputs as: $A_{3}, A_{2}, A_{1}, A_{0}$. Label the output as: $f$.
(2) Write the Boolean expression for $f$, and simplify it.
$\qquad$
(3) Implement the circuit with a 4-1 MUX. Label input and selector lines.


